Study Guide

KeyConcepts

Points, Lines, and Planes (Lesson 1-1)

- There is exactly one line through any two points.
- There is exactly one plane through any three noncollinear points.

Distance and Midpoints (Lesson 1-3)

- On a number line, the measure of a segment with endpoint coordinates a and b is $|a - b|$.
- In the coordinate plane, the distance between two points (x_1, y_1) and (x_2, y_2) is given by $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$.
- On a number line, the coordinate of the midpoint of a segment with endpoints a and b is $\dfrac{a + b}{2}$.
- In the coordinate plane, the coordinates of the midpoint of a segment with endpoints that are (x_1, y_1) and (x_2, y_2) are $\left(\dfrac{x_1 + x_2}{2}, \dfrac{y_1 + y_2}{2}\right)$.

Angles (Lessons 1-4 and 1-5)

- An angle is formed by two noncollinear rays that have a common endpoint, called its vertex. Angles can be classified by their measures.
- Adjacent angles are two coplanar angles that lie in the same plane and have a common vertex and a common side but no common interior points.
- Vertical angles are two nonadjacent angles formed by two intersecting lines.
- A linear pair is a pair of adjacent angles with noncommon sides that are opposite rays.
- Complementary angles are two angles with measures that have a sum of 90.
- Supplementary angles are two angles with measures that have a sum of 180.

FOLDABLES StudyOrganizer

Be sure the Key Concepts are noted in your Foldable.

KeyVocabulary

- acute angle (p. 38)
- adjacent angles (p. 46)
- angle (p. 36)
- angle bisector (p. 39)
- area (p. 58)
- base (p. 67)
- between (p. 15)
- circumference (p. 58)
- collinear (p. 5)
- complementary angles (p. 47)
- concave (p. 56)
- cone (p. 67)
- congruent (p. 16)
- construction (p. 17)
- convex (p. 56)
- coplanar (p. 5)
- cylinder (p. 67)
- degree (p. 37)
- distance (p. 25)
- edge (p. 67)
- equiangular polygon (p. 57)
- equilateral polygon (p. 57)
- exterior (p. 36)
- face (p. 67)
- interior (p. 36)
- intersection (p. 6)
- line (p. 5)
- line segment (p. 14)
- linear pair (p. 46)
- midpoint (p. 27)
- n-gon (p. 57)
- obtuse angle (p. 38)
- opposite rays (p. 36)
- perimeter (p. 58)
- perpendicular (p. 48)
- plane (p. 5)
- Platonic solid (p. 68)
- point (p. 5)
- polygon (p. 56)
- polyhedron (p. 67)
- prism (p. 67)
- pyramid (p. 67)
- ray (p. 36)
- regular polygon (p. 57)
- regular polyhedron (p. 68)
- right angle (p. 38)
- segment bisector (p. 29)
- side (p. 36)
- space (p. 7)
- sphere (p. 67)
- supplementary angles (p. 47)
- surface area (p. 69)
- undefined term (p. 5)
- vertex (pp. 36, 67)
- vertex of a polygon (p. 56)
- vertical angles (p. 46)
- volume (p. 69)

VocabularyCheck

Fill in the blank in each sentence with the vocabulary term that best completes the sentence.

1. A _____ is a flat surface made up of points that extends infinitely in all directions.

2. A set of points that all lie on the same line are said to be _____.

3. If two lines intersect to form four right angles, the lines are called _____.

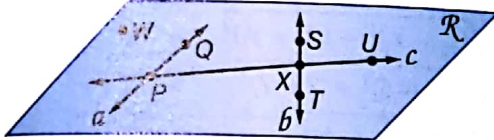4. If the sum of the measures of two angles is 180, then the angles are called _____ angles.
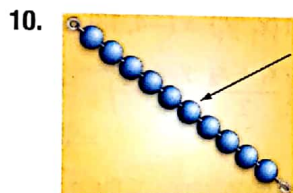
Lesson-by-Lesson Review

1-1 Points, Lines, and Planes (pp. 5–12)
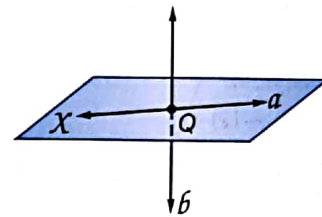
Use the figure to complete each of the following.

5. Name the intersection of lines a and c.

6. Give another name for line b.

7. Name a point that is not contained in any of the three lines a, b, or c.

8. Give another name for plane WPX.

Name the geometric term that is best modeled by each item.

9.

10.

Example 1

Draw and label a figure for the relationship below.

Plane X contains line a, line b intersects line a at point Q, but line b is not in plane X.

Draw a surface to represent plane X and label it.

Draw a line in plane X and label it line a.

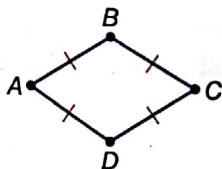Draw a line b intersecting both the plane and line a and label the point of intersection Q.

1-2 Linear Measure (pp. 14–21)

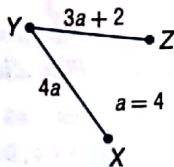Find the value of the variable and XP, if X is between P and Q.

11. $XQ = 13$, $XP = 5x - 3$, $PQ = 40$

12. $XQ = 3k$, $XP = 7k - 2$, $PQ = 6k + 16$

Determine whether each pair of segments is congruent.
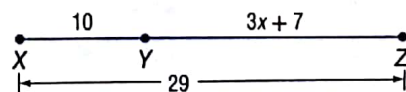
13. $\overline{AB}$, $\overline{CD}$

14. $\overline{XY}$, $\overline{YZ}$

15. **DISTANCE** The distance from Salvador's job to his house is 3 times greater than the distance from his house to school. If his house is between his job and school and the distance from his job to school is 6 miles, how far is it from Salvador's house to school?

Example 2

Use the figure to find the value of the variable and the length of $\overline{YZ}$.

$XZ = XY + YZ$	Betweenness of points	
$29 = 10 + 3x + 7$	Substitution	
$29 = 3x + 17$	Simplify.	
$12 = 3x$	Subtract 17 from each side.	
$4 = x$	Divide each side by 3.	
$YZ = 3x + 7$	Given	
$\quad = 3(4) + 7$ or 19	Substitution	

So, $x = 4$ and $YZ = 19$.

1-3 Distance and Midpoints (pp. 25-35)

Find the distance between each pair of points.

16. $A(-3, 1)$, $B(7, 13)$

17. $P(2, -1)$, $Q(10, -7)$

Find the coordinates of the midpoint of a segment with the given endpoints.

18. $L(-3, 16)$, $M(17, 4)$

19. $C(32, -1)$, $D(0, -12)$

Find the coordinates of the missing endpoint if M is the midpoint of $\overline{XY}$.

20. $X(-11, -6)$, $M(15, 4)$

21. $M(-4, 8)$, $Y(19, 0)$

22. HIKING Carol and Marita are hiking in a state park and decide to take separate trails. The map of the park is set up on a coordinate grid. Carol's location is at the point $(7, 13)$ and Marita is at $(3, 5)$.

   a. Find the distance between them.

   b. Find the coordinates of the point midway between their locations.

Example 3

Find the distance between $X(5, 7)$ and $Y(-7, 2)$.

Let $(x_1, y_1) = (5, 7)$ and $(x_2, y_2) = (-7, 2)$.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$
$$= \sqrt{(-7 - 5)^2 + (2 - 7)^2}$$
$$= \sqrt{(-12)^2 + (-5)^2}$$
$$= \sqrt{169} \text{ or } 13$$

The distance from X to Y is 13 units.

Example 4

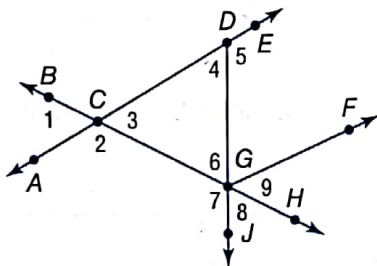Find the coordinates of the midpoint between $P(-4, 13)$ and $Q(6, 5)$.

Let $(x_1, y_1) = (-4, 13)$ and $(x_2, y_2) = (6, 5)$.

$$M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right) = M\left(\frac{-4 + 6}{2}, \frac{13 + 5}{2}\right)$$
$$= M(1, 9)$$
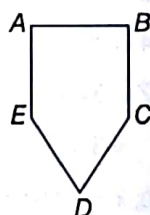
The coordinates of the midpoint are $(1, 9)$.

1-4 Angle Measure (pp. 36-44)

For Exercises 23-26, refer to the figure below.

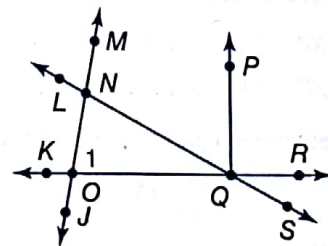**23.** Name the vertex of $\angle 7$.

24. Write another name for $\angle 4$.

25. Name the sides of $\angle 2$.

26. Name a pair of opposite rays.

27. SIGNS A sign at West High School has the shape shown. Measure each of the angles and classify them as *right*, *acute*, or *obtuse*.

Example 5

Refer to the figure below. Name all angles that have Q as a vertex.

$\angle OQN$, $\angle NQP$, $\angle PQR$, $\angle RQS$, $\angle SQO$, $\angle OQP$, $\angle NQR$, $\angle PQS$, $\angle OQR$
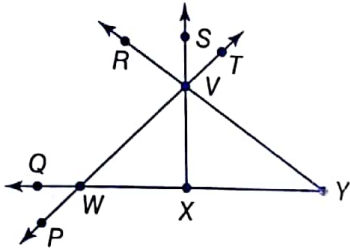
Example 6

In the figure above, list all other names for $\angle 1$.

$\angle NOQ$, $\angle QON$, $\angle MOQ$, $\angle QOM$, $\angle MOR$, $\angle ROM$, $\angle NOR$, $\angle RON$

1-5 Angle Relationships (pp. 46–54)

For Exercises 28–30, refer to the figure below.

28. Name an angle supplementary to $\angle TVY$.

29. Name a pair of vertical angles with vertex W.

30. If $m\angle SXW = 5x - 16$, find the value of x so that $\overrightarrow{SX} \perp \overleftrightarrow{WY}$.

31. PARKING The parking arm shown below rests in a horizontal position and opens to a vertical position. After the arm has moved 24°, how many more degrees does it have to move so that it is vertical?

Example 7

Name a pair of supplementary angles and a pair of complementary angles in the figure below.
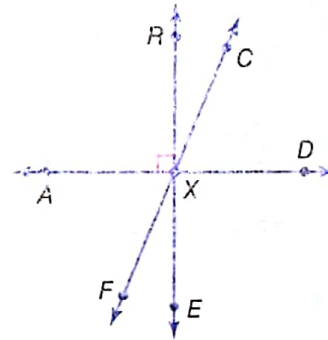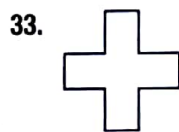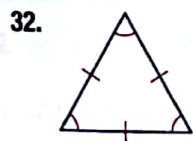

Sample answers:

Supplementary angles: $\angle RXA$ and $\angle RXD$

Complementary angles: $\angle RXC$ and $\angle CXD$

## 1-6 Two-Dimensional Figures (pp. 56–64)

Name each polygon by its number of sides. Then classify it as *convex* or *concave* and *regular* or *irregular*.

32.

33.

34. Find the perimeter of quadrilateral $ABCD$ with vertices $A(-3, 5)$, $B(0, 5)$, $C(2, 0)$, and $D(-5, 0)$.

35. PARKS Westside Park received 440 feet of chain-link fencing as a donation to build an enclosed play area for dogs. The park administrators need to decide what shape the area should have. They have three options: (1) a rectangle with length of 100 feet and width of 120 feet, (2) a square with sides of length 110 feet, or (3) a circle with radius of approximately 70 feet. Find the areas of all three enclosures and determine which would provide the largest area for the dogs.

Example 8

Name the polygon by its number of sides. Then classify it as *convex* or *concave* and *regular* or *irregular*.
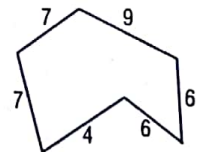
There are 6 sides, so this is a hexagon. If two of the sides are extended to make lines, they will pass through the interior of the hexagon, so it is concave. Since it is concave, it cannot be regular.

Example 9

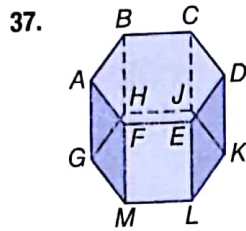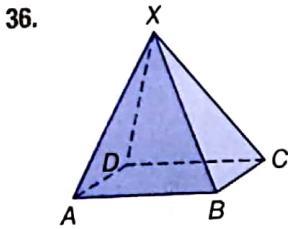Find the perimeter of the polygon in the figure above.

$P = s_1 + s_2 + s_3 + s_4 + s_5 + s_6$ Definition of perimeter

$= 7 + 7 + 9 + 6 + 6 + 4$ Substitution

$= 39$ Simplify.
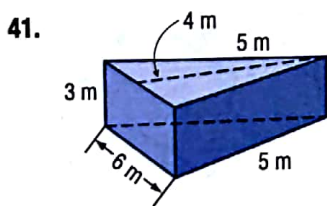
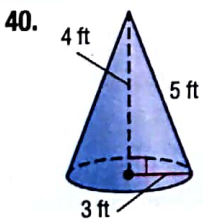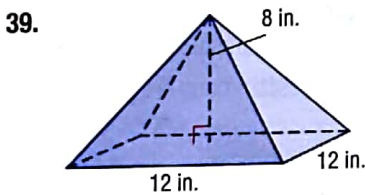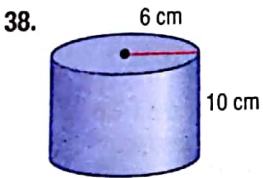The perimeter of the polygon is 39 units.

1-7 Three-Dimensional Figures (pp. 67–74)

Identify each solid. Name the bases, faces, edges, and vertices.

36.

37.

Find the surface area and volume of each solid.

38. 6 cm, 10 cm

39. 8 in., 12 in., 12 in.

40. 4 ft, 5 ft, 3 ft

41. 4 m, 5 m, 3 m, 6 m, 5 m

**42. BUILDING** Chris is building a trunk like the one shown below. His design is a square prism. What is the volume of the trunk?

2 ft, 3 ft, 3 ft

43. HOCKEY A regulation hockey puck is a cylinder made of vulcanized rubber 1 inch thick and 3 inches in diameter. Find the surface area and volume of a hockey puck.

Example 10

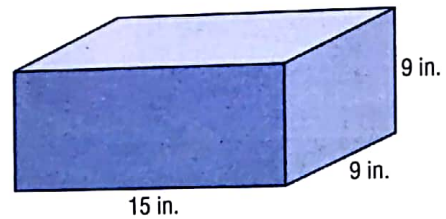Identify the solid below. Name the bases, faces, edges, and vertices.
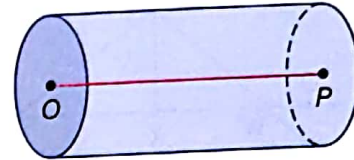
This solid has congruent circular bases in a pair of parallel planes. So, it is a cylinder.

Bases: circle O and circle P

A cylinder has no faces, edges, or vertices.

Example 11

Find the surface area and volume of the rectangular prism below.

9 in., 9 in., 15 in.

$T = Ph + 2B$	Surface area of a prism
$\ = (48)(9) + 2(135)$	Substitution
$\ = 702$	Simplify.

The surface area is 702 square inches.

$V = Bh$	Volume of a prism
$\ = (135)(9)$	Substitution
$\ = 1215$	Simplify.

The volume is 1215 cubic inches.

Use the figure to name each of the following.
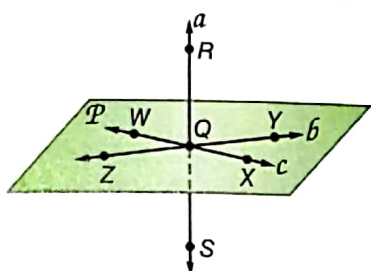
1. the line that contains points Q and Z

2. two points that are coplanar with points W, X, and Y

3. the intersection of lines a and b

**Find the value of the variable if P is between J and K.**

4. $JP = 2x$, $PK = 7x$, $JK = 27$

5. $JP = 3y + 1$, $PK = 12y - 4$, $JK = 75$

6. $JP = 8z - 17$, $PK = 5z + 37$, $JK = 17z - 4$

Find the coordinates of the midpoint of a segment with the given endpoints.
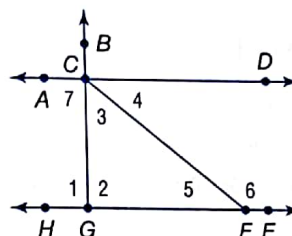
7. $(16, 5)$ and $(28, -13)$

8. $(-11, 34)$ and $(47, 0)$

9. $(-4, -14)$ and $(-22, 9)$

Find the distance between each pair of points.

10. $(43, -15)$ and $(29, -3)$

11. $(21, 5)$ and $(28, -1)$

12. $(0, -5)$ and $(18, -10)$

13. **ALGEBRA** The measure of $\angle X$ is 18 more than three times the measure of its complement. Find the measure of $\angle X$.

14. Find the value of x that will make lines a and b perpendicular in the figure below.
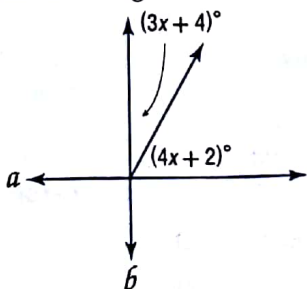
For Exercises 15–18, use the figure below.

15. Name the vertex of $\angle 3$.

16. Name the sides of $\angle 1$.

17. Write another name for $\angle 6$.

18. Name a pair of angles that share exactly one point.

19. **MULTIPLE CHOICE** If $m\angle 1 = m\angle 2$, which of the following statements is true?

   A $\angle 2 \cong \angle 4$

   B $\angle 2$ is a right angle.

   C $\ell \perp m$

   D All of the above
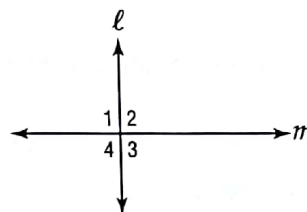
Find the perimeter of each polygon.

20. triangle XYZ with vertices $X(3, 7)$, $Y(-1, -5)$, and $Z(6, -4)$

21. rectangle $PQRS$ with vertices $P(0, 0)$, $Q(0, 7)$, $R(12, 7)$, and $S(12, 0)$

22. **SAFETY** A severe weather siren in a local city can be heard within a radius of 1.3 miles. If the mayor of the city wants a new siren that will cover double the area of the old siren, what should the radius of the new siren be? Round to the nearest tenth of a mile.

Refer to the figure at the right.

23. Name the base.

24. Find the surface area.

25. Find the volume.

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